

pg. 333 # 13-29 odd +20

13. Square roots come in \pm pairs!
 $-\sqrt{5}$ & $\sqrt{13}$ are other roots

19. 1 and $\pm 3i$. $-3i$ is other root

roots: 1 $3i$ $-3i$
 factors: $(x-1)$ $(x-3i)$ $(x+3i)$

$$x^2 - 9i^2 = x^2 - 9(-1) = x^2 + 9$$

	x^3	$9x$
x		
-1	$-x^2$	-9

$$x^3 - x^2 + 9x - 9$$

25. $\frac{6}{12} \pm \frac{1}{\pm 1} \pm \frac{2}{\pm 2} \pm \frac{3}{\pm 3} \pm \frac{4}{\pm 4} \pm \frac{6}{\pm 6} \pm \frac{12}{\pm 12}$

	possible roots	y	
look in table	1	-7	
	-1	-75	
	2	12	
	-2	-280	
	3	105	
	-3	-693	
	6	1584	
	-6	-3900	
	STO	$\frac{1}{2}$	0
		$-\frac{1}{2}$	-28
$\frac{3}{2}$		0	
$-\frac{3}{2}$		-156	
$\frac{1}{3}$		$-\frac{7}{9}$	
$-\frac{1}{3}$		$-\frac{55}{3}$	
$\frac{2}{3}$		0	
$-\frac{2}{3}$		$-\frac{364}{9}$	

possible roots	y
$\frac{1}{4}$	-1.5625
$-\frac{1}{4}$	-14.44
$\frac{3}{4}$	-1.875
$-\frac{3}{4}$	-47.81
$\frac{1}{6}$	-
$-\frac{1}{6}$	-
$\frac{1}{12}$	-
$-\frac{1}{12}$	-

actual roots
 $\frac{1}{2}, \frac{2}{2}, \frac{2}{3}$

$$(2x-1)(2x-3)(3x-2)$$

$$12x^3 \dots - 6$$

29. $3+i$ & $3-i$, $-2i$ & $2i$ ← roots

$(x-(3+i))(x-(3-i))(x+2i)(x-2i)$ ← factors

	x	$-3-i$
x	x^2	$-3x-ix$
$-3+i$	$-3x+ix$	$9+1$

D2D

$$x^2 - 4i^2 = x^2 + 4$$

	$x^2 - 6x + 10$		
x^2	x^4	$-6x^3$	$10x^2$
4	$4x^2$	$-24x$	40

$$x^4 - 6x^3 + 14x^2 - 24x + 40$$

Answers for Lesson 6-5, pp. 333–334 Exercises

1. $\pm 1, \pm 2; 1$
 2. $\pm 1, \pm 2, \pm 3, \pm 6; 1, -2, -3$
 3. $\pm 1, \pm 2, \pm 4; -1$
 4. $\pm \frac{1}{2}, \pm 1, \pm 2, \pm 4, \pm 8; \text{no rational roots}$
 5. $\pm 1, \pm 2, \pm 4, \pm 8, \pm 16; -2$
 6. $\pm 1, \pm 3, \pm 5, \pm 15; \text{no rational roots}$
 7. $2, \pm i\sqrt{5}$
 8. $5, \pm i\sqrt{7}$
 9. $-3, 1, \frac{7}{2}$
 10. $-5, \frac{1 \pm \sqrt{3}}{2}$
 11. $\pm \frac{1}{2}, \pm 3$
 12. $1, -2, \frac{1 \pm \sqrt{7}}{3}$

12

13. $-\sqrt{5}, \sqrt{13}$
 14. $4 + \sqrt{6}, -\sqrt{3}$
 15. $1 + \sqrt{10}, 2 - \sqrt{2}$
 16. $1 - i, 5i$
 17. $2 - 3i, -6i$
 18. $4 + i, 3 - 7i$
 19. $x^3 - x^2 + 9x - 9 = 0$
 20. $x^3 + 3x^2 - 8x + 10 = 0$
 21. $x^3 - 2x^2 + 16x - 32 = 0$
 22. $x^3 - 3x^2 - 8x + 30 = 0$
 23. $x^3 - 6x^2 + 4x - 24 = 0$
 24. $x^3 - x^2 + 2 = 0$
 25. $\pm \frac{1}{12}, \pm \frac{1}{6}, \pm \frac{1}{4}, \pm \frac{1}{2}, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{3}{4}, \pm 1, \pm \frac{3}{2}, \pm 2, \pm 3, \pm 6; \frac{1}{2}, \frac{3}{2}, \frac{2}{3}$
 26. $\pm \frac{1}{10}, \pm \frac{1}{5}, \pm \frac{2}{5}, \pm \frac{1}{2}, \pm \frac{4}{5}, \pm 1, \pm 2, \pm \frac{5}{2}, \pm 4, \pm 5, \pm 10, \pm 20; 2, \frac{2}{5}, \frac{5}{2}$
 27. $\pm \frac{7}{3}, \pm \frac{1}{6}, \pm \frac{1}{2}, \pm \frac{1}{3}, \pm \frac{7}{6}, \pm 1, \pm \frac{3}{2}, \pm 3, \pm \frac{7}{2}, \pm 7, \pm \frac{21}{2}, \pm 21; \frac{1}{3}, -\frac{7}{2}, 1, 3$
 28. $\pm \frac{1}{4}, \pm \frac{5}{4}, \pm \frac{1}{2}, \pm \frac{3}{4}, \pm \frac{1}{8}, \pm \frac{5}{8}, \pm \frac{3}{8}, \pm \frac{15}{4}, \pm \frac{5}{2}, \pm 1, \pm \frac{3}{2}, \pm \frac{15}{8}, \pm \frac{15}{2}, \pm 15, \pm 3, \pm 5; -\frac{1}{2}, \frac{3}{2}, \frac{5}{2}$
 29. $x^4 - 6x^3 + 14x^2 - 24x + 40 = 0$
 30. $x^4 - 2x^3 - x^2 + 6x - 6 = 0$
 31. $x^4 - 6x^3 + 2x^2 + 30x - 35 = 0$

11